Contact Stress Analysis of Spiral Bevel Gears Using Nonlinear Finite Element Static Analysis

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Prepared for the 29th Joint Propulsion Conference and Exhibit cosponsored by the AIAA, SAE, ASME, and ASEE Monterey, California, June 28–30, 1993

NASA-TM-106176) CONTACT STRESSINALYSIS OF SPIRAL BEVEL GEARSISING NONLINEAR FINITE ELEMENT STATIC ANALYSIS (NASA) 12 p





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Abstract

A procedure is presented for performing threedimensional stress analysis of spiral bevel gears in mesh using the finite element method. The procedure involves generating a finite element model by solving equations that identify tooth surface coordinates. Coordinate transformations are used to orientate the gear and pinion for gear meshing. Contact boundary conditions are simulated with gap elements. A solution technique for correct orientation of the gap elements is given. Example models and results are presented.

Introduction

Spiral bevel gears are used to transmit power between intersecting shafts. One such application is in helicopter transmission systems. In this critical application, the gears operate at relatively high rotational speed and transmit substantial power (i. e. 1500 HP at 21,000 rpm).

Prior research has focused on spiral bevel gear geometry¹⁻⁶ to reduce vibration and kinematic error, improve manufacturability and improve inspection. Stress analysis is another important area of ongoing research. Accurate prediction of contact stresses and tooth root/fillet stresses are important to increase reliability and reduce weight.

Much effort has focused on predicting stresses in gears with the finite element method. Most of this work has involved parallel axis gears with two dimensional models. Only a few researchers have investigated finite element analysis of spiral bevel gears^{7,8}.

Finite element analysis has been done on a single spiral bevel tooth using an assumed contact stress distribution?. The research reported here will utilize the numerical solution for spiral bevel surface geometry to study gear meshing. Pinion tooth and gear tooth surfaces will be developed based on the gear manufacturing kinematics. The individual teeth are then rotated in space to create a multi-tooth model (4 gear and 3 pinion teeth). The tooth pair contact zones are modeled with gap elements. The model development procedure and finite element results are presented.

Equations for Tooth Surface Coordinates

The system of equations, briefly summarized here, rerequired to define the coordinates of a face-milled spiral bevel gear surface were developed by Handschuh and Litvin⁹.

A conical cutting head, attached to a rotating cradle, swings through the work piece. Parameters U and θ locate a point on the cutting head in coordinate system S_c attached to the cutting head as shown in figure 1 and

described by the following equations.

$$r_{c} = \begin{cases} r \cot \psi - U \cos \psi \\ U \sin \psi \sin \theta \\ U \sin \psi \cos \theta \\ 1 \end{cases}$$
 (1)

The roll angle of the cradle ϕ_c is used to locate the rotating cradle with respect to the fixed machine coordinate system S_m . Parameters U, θ and ϕ_c , along with various machine tool settings can be used to completely define the location of a point on the cutting head in space.

Since the kinematic motion of cutting a gear is equivalent to the cutting head meshing with a simulated crown gear, an equation of meshing can be written in terms of a point on the cutting head (i.e., in terms of U, θ and ϕ_o). The equation of meshing for straight-sided cutters with a constant ratio of roll between the cutter and work piece is given in^{1,5,6} as:

(U -
$$\tau \cot \psi \cos \psi$$
) $\cos \gamma \sin \tau + S(m_{cw} - \sin \gamma)$
 $\cos \psi \sin \theta \mp \cos \gamma \sin \gamma \sin (q - \phi_c)]$
 $\pm E_m (\cos \gamma \sin \psi + \sin \gamma \cos \psi \cos \tau)$
 $- L_m \sin \gamma \cos \psi \sin \tau = 0$ (2)

The upper and lower signs are for left and right hand gears respectively. The following machine tool settings are defined 5,6,9.

cutting blade angle $(\theta \mp q \pm \phi)$ cradle angle root angle of work piece machining offset vector sum of change of machine center to back and the sliding base ϕ_c/ϕ_w , the relationship between m_ the cradle and work piece for a constant ratio of roll U generating cone surface coordinate S radial location of cutting head in coordinate system S_m radius of generating cone surface

This is equivalent to:

$$f_1(U, \theta, \phi_c) = 0 \tag{3}$$

Because there are 3 unknowns U, θ , and ϕ_c ; three equations must be developed to solve for the surface

coordinates of a spiral bevel gear. The 3 parameters U, θ and ϕ_c are defined relative to the cutting head and cradle coordinate systems (S_c and S_s) respectively. These parameters can be transformed through a series of coordinate transformations to a coordinate system attached to the work piece. Or U, θ , ϕ_c can be mapped into X_w , Y_w , Z_w in coordinate system S_w attached to the work piece. These transformations, used in conjunction with two other geometric requirements, give the two additional equations.

The correct U, θ and ϕ_c that solves the equation of meshing, must also, upon transformation to the work piece coordinate system S_w , result in a axial coordinate Z_w that matches with a preselected axial position Z. (See figure 2)

$$Z_{-} - Z = 0 \tag{4}$$

This equation along with the correct coordinate transformations (see equation 11) result in a second equation of the form

$$f_2(U,\theta,\phi_c) = 0 (5)$$

A similar requirements for the radial location of a point on the work piece results in (See figure 2).

$$r - (X_w^2 + Y_w^2)^{1/2} = 0$$
(6)

The appropriate coordinate transformations (see equation 11) will convert equation (6) into a function of U, θ , and ϕ_c .

$$f_3(U,\theta,\phi_a) = 0 (7)$$

Equations (3), (5) and (7) form the system of nonlinear equations necessary to define a point on the tooth surface.

Solution Technique

An initial guess U°, θ °, ϕ_c ° is used to start iterative solution procedures. Newton's method is used to determine subsequent values of the updated vector (U^k, θ ^k, ϕ_c ^k)¹⁰.

Where the vector Y is the solution of:

$$\begin{bmatrix} \frac{\partial f_{1}(U^{k-1})}{\partial U} & \frac{\partial f_{1}(\theta^{k-1})}{\partial U} & \frac{\partial f_{2}(\phi_{c}^{k-1})}{\partial \phi_{c}} \\ \frac{\partial f_{2}(U^{k-1})}{\partial U} & \frac{\partial f_{2}(\theta^{k-1})}{\partial U} & \frac{\partial f_{2}(\phi_{c}^{k-1})}{\partial \phi_{c}} \\ \frac{\partial f_{3}(U^{k-1})}{\partial U} & \frac{\partial f_{3}(\theta^{k-1})}{\partial U} & \frac{\partial f_{3}(\phi_{c}^{k-1})}{\partial \phi_{c}} \end{bmatrix} \cdot \begin{bmatrix} Y_{1}^{k-1} \\ Y_{2}^{k-1} \\ Y_{3}^{k-1} \end{bmatrix}$$

$$= \begin{cases} f_{1}(U^{k-1}, \theta^{k-1}, \phi_{c}^{k-1}) \\ f_{2}(U^{k-1}, \theta^{k-1}, \phi_{c}^{k-1}) \\ f_{3}(U^{k-1}, \alpha^{k-1}, \phi_{c}^{k-1}) \end{cases}$$
(9)

The 3x3 matrix in the preceding equation is the Jacobian matrix and must be inverted each iteration to solve for the Y vector. The equation of meshing, function f_1 is numerically differentiated directly to find the terms for the Jacobian matrix. Function f_2 and f_3 can not be directly differentiated with respect to U, θ and ϕ_c . After each iteration $U^{k\cdot l}$, $\theta^{k\cdot l}$, $\phi_c^{k\cdot l}$ (in the cutting head coordinate system Sc) are transformed into the work piece coordinate system, S_w , with the series of coordinate transformations as given in equation 11.

$$\begin{cases} X_{w} \\ Y_{w} \\ Z_{w} \\ 1 \end{cases} = \begin{bmatrix} M_{wc} \end{bmatrix} \quad \begin{cases} r \cot \psi - U \cos \psi \\ U \sin \psi \sin \theta \\ U \sin \psi \cos \theta \end{cases}$$
 (10)

where:

$$[M_{wc}] = [M_{wa} f(\phi_c)] [M_{gg}] [M_{gg}] [M_{gg} f(\phi_c)] [M_{sc}]_{(11)}$$

Each matrix [M] above represents a transformation from one coordinate system to another. (See Appendix I for the specific matrices.)

Functions f_2 and f_3 are evaluated by starting with an initial U^k , θ^k and ϕ_c^k , performing the transformation in equation 11 and evaluating equations (4) and (6). The numerical differentiation of f_2 and f_3 is performed by transforming U^k + inc, θ^k + inc, ϕ_c^k + inc (where inc is a small increment appropriate for

numerical differentiation into $X_w + \text{inc}$, $Y_w + \text{inc}$, $Z_w + \text{inc}$. Equations (4) and (6) are then used to evaluate the numerical differentiation. Function f_1 , f_2 , f_3 and the partial derivatives of f_1 , f_2 , f_3 required to the Jacobian matrix are updated each iteration. The iteration continues until the Y vector is less than a predetermined tolerance. This completes the solution techniques for a single point on the spiral bevel gear surface.

The four corners of the active profile are identified from the tooth geometry plane as shown in figure 2. Point 1 on the surface is chosen to be the lowest point of the active profile on the toe end. The initial guess to start the procedure has to be sufficiently close to the correct solution for convergence to occur. The solution for the first point proves to be an adequate initial guess for any subsequent points on the surface.

Subsequent interior surface points are found by incrementing $r = (X^2 + Y^2)^{1/2}$ and Z. By adjusting the increments used, a surface mesh of any density can be calculated. The process is repeated four times for each of four surfaces; gear convex, gear concave, pinion convex and pinion concave.

Since all four surfaces are generated independently, additional matrix transformations are required to obtain the appropriate orientation for meshing. The proper convex and concave surface orientation (for both the gear and pinion) is found by fixing the concave surface and rotating the convex surface until the correct tooth thickness is obtained. The correct angle of rotation is obtained by matching the tooth top land thickness with the desired value.

Gear and Pinion Orientations Required For Meshing

After generating the pinion and gear surface as described above, the pinion cone and gear cone apex will meet at the same point as shown in figure 3. This point is the origin of the fixed coordinate system attached to the work piece being generated. To place the gear and pinion in mesh with each other rotations described in the following example are required:

- 1. The 19th tooth is selected for meshing. This corresponds to rotating the generated tooth 190° CW about the Z_w axis. (For this example, $N_t = 36$ total teeth on the gear.) For the general case the gear tooth is rotated $360/N_t + 180^\circ$ CW about its axis of rotation (Z_w) . This corresponds to selecting the ith tooth of the gear to be in mesh where $i = N_t/2 + 1$.
- 2. The pinion is rotated by 90° CCW about the Y axis.

Note: rotation (1) corresponds to selecting a different tooth on the gear to be in mesh; however, rotation (2) corresponds to physically rotating the entire pinion until it meshes with the gear.

3. Because the four surfaces are derived independently, their orientation is random with respect to meshing. The physical location of the gear and pinion after rotations (1) and (2) correspond to the gear and pinion in mesh with severe interference. To correct the interference the pinion is rotated CW about its axis of rotation (Z_w) until surface contact occurs. For this example the rotation was 3.56°. Figure 4 shows an example of a simulated gear pair meshing. The generated pinion tooth was copied and rotated 12 times and the generated gear tooth was copied and rotated 36 times.

Contact Simulation

The tooth pair mesh contact point can be located by a method described by Litvin⁶ or by a search technique. Pairs of finite element node points (one on each tooth surface) are evaluated until the pair with smallest separation distance is obtained. (A finer finite element mesh would yield greater resolution.) Once the contact point is established, a vector normal to the surface at the contact point is calculated.

The intersection of the normal vector on the pinion at the contact point with the gear surface identifies the second point required to define the gap element. Additional gap elements are obtained by taking additional vectors from other pinion surface finite element nodal points (parallel to the contact point normal vector), and calculating where they intersect the mating gear surface. Finite element nodal points on the gear surface are located to the intersection points of the normal vectors and the gear tooth surface.

The vector normal to the cutting surface is given in⁵ as:

$$\{ n_{m} \} = \begin{cases} \sin \psi_{c} \\ \cos \psi_{c} \sin \tau \\ \cos \psi_{c} \cos \tau \end{cases}$$
 (12)

This vector is written relative to S_e , a coordinate system fixed to the cutting head. To obtain the vector n_w relative to the coordinate system fixed to the work piece, the following transformation must be performed.

$$\{\mathbf{n}_{w}\} = [\mathbf{L}_{wc}]\{\mathbf{n}_{m}\} \tag{13}$$

Where $[L_{wc}]$ is found by removing the 4th row and column from $[M_{wc}]$.

Each gap element is connected between a node on the pinion surface, hereafter designated node 1, and the corresponding intersection node point on the gear surface, designated node 2. The intersection point on the gear surface is found as follows:

Consider node 1, a point on the pinion with coordinates P_x , P_y , P_z in S_w . Let Q_x , Q_y , Q_z be any point in space such that $(Q_x, Q_y, Q_z)^t = b(n_x, n_y, n_z)^t$ where b is a scale factor, and n_x , n_y and n_z are the components of the normal vector at the contact point. The intersection of the normal vector from node 1 with the mating gear surface defines node 2 and has to satisfy the following three equations:

$$Q_x = G_x = X_p + b n_x$$

 $Q_y = G_y = X_p + b n_y$
 $Q_x = G_z = Z_p + b n_z$
(14)

Where G_x , G_y , G_z is a point on the gear surface. A point on the gear surface must also satisfy

$$\begin{cases}
G_x \\
G_y \\
G_z
\end{cases} = [M_{wc}] \begin{cases}
r \cos \psi_c - U \cos \psi_c \\
U \sin \psi_c \sin \theta \\
U \sin \psi_c \cos \theta \\
1
\end{cases} (15)$$

Equation 15 leads to a system of 3 nonlinear algebraic equations. These three equations, along with the equation of meshing for the gear surface provide a system of 4 equations and 4 unknowns (u, θ , ϕ_e , b). these equations are solved with Newton's method described earlier. The intersection of the normal from node 1 on the pinion with the gear surface is now obtained.

This procedure is used to locate the intersection of normals from all points on the pinion surface (in the contact zone) with the gear surface. The gear tooth surface is remeshed utilizing the intersection points as shown in figure 5. Gap elements are connected between corresponding nodal points on the pinion and the intersection points on the gear surface.

Finite Element Model

An example analysis was performed using gears from the NASA Lewis Spiral Bevel Gear Test Facility. In this case, the left hand pinion mates with the right hand gear. Counter clockwise rotation of the pinion results in the concave surface on the pinion mating with the convex gear surface.

The design data for the pinion and gear are given in Table I. The design data are used with methods given in 6 to determine the machine tool settings for the straight sided cutter data given in Table II.

The finite element gear pair model, shown in figure 6, contains 4 gear teeth and three pinion teeth. The model had 10,101 nodes (30,303 degrees of freedom) and 7596 eight noded 3D brick elements.

The three pinion teeth are fixed in space with zero displacements and rotations. This is done by setting x, y and z displacements equal to zero on the four corner nodes of each rim section. The gear is constrained to rotation about its axis of rotation. The gear is loaded with a torque of 9450 in lbs on the gear by applying 4725 lb force located 2.0976" from the gear axis of rotation.

At the orientation chosen between the pinion and gear two pairs of teeth were in contact. One pair had contact near the middle region of the tooth and another pair had contact near the toe (i.e., about to go out of mesh). Initially the model started with a total of twenty one gap elements. For the tooth that is approximately midway through mesh, fifteen gap elements were used. For the tooth about to leave mesh, four gap elements were used. The analysis starts with one gap elements closed in each contact zone. Within the finite element code an iterative process is used to determine how many gap elements must close to reach static equilibrium. The solution iterated four times before reaching equilibrium with four gap element closed in the main contact region and one closed in the edge contact region. Stress contours for the two pinion teeth with contact are shown in Figures 7 and 8.

The average nodal minimum principal stresses in the main contact zone average -204,000 psi with a maximum of -299,900 psi and a minimum of -103,574 psi. The corresponding elemental stresses average -103,500 psi with a maximum and minimum of -123,900 psi and -79,500 psi, respectively. Thenodal stresses are higher because of load

concentration from the gap elements. These stress ranges bracket the estimated hertzian stresses for the gear set under the same load conditions. Contact with only 4 gap elements, along with large stress gradient among adjacent nodes indicate the need for a finer finite element mesh for improved stress prediction.

Conclusions

A multi tooth finite element model was used to perform three-dimensional contact analysis of spiral bevel gears in mesh. Four gear teeth and three pinion teeth are generated by solving the equations, based on gear manufacturing kinematics, that identify tooth surface coordinates. The gear and pinion are orientated for meshing with coordinate transformations.

Surface stresses are evaluated with gap elements. The gear surface is remeshed with nodal points relocated to identify the correct gap element orientation. Initial FEA stress results compare favorably with calculated hertzian contact stresses. However; large stress gradients between adjacent nodes in the contact zones indicate a need for greater finite element mesh refinement.

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Appendix I

Coordinate transformations involving both rotation and translation require mixed matrix operations of multiplication and addition. Matrix representation of coordinate transformations will need only multiplication of matrices if position vectors are represented by homogeneous coordinates. The following 4 x 4 matrices are required to transform the homogeneous coordinates of a point on the cutting head to a point on the work piece.

Matrix [M_{sc}] transforms coordinate system S_c, attached to the cutting head, into system S_s, rigidly connected to the cradle.

$$[M_{x}] = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos q & \mp \sin q & \mp \sin q \\ 0 & \pm \sin q & \cos q & s \cos q \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
(16)

Matrix $[M_{ms}]$ transforms coordinate system S_s into system S_m attached to the frame.

$$[M_{ms}] = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \phi_c & \mp \sin \phi_c & 0 \\ 0 & \pm \sin \phi_c & \cos \phi_c & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
(17)

Matrix $[M_{np}]$ transforms coordinate system S_n into system S_p which orientates the apex of the gear being manufactured.

$$[M_{pm}] = \begin{bmatrix} \cos \delta & 0 & -\sin \delta & -L_{m} \sin \delta \\ 0 & 1 & 0 & \pm E_{m} \\ \sin \delta & 0 & \cos \delta & L_{m} \cos \delta \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
(18)

Matrix $[M_{ap}]$ transforms coordinate system S_p into system S_a which located the apex of the gear being manufacturer with respect to S_m

$$[M_{ap}] = \begin{bmatrix} \cos \mu & 0 & \sin \mu & 0 \\ \mp \sin \phi_w & \cos \phi_w & 0 & 0 \\ -\sin \mu & 0 & \cos \mu & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
(19)

Matrix [M_{wa}] transforms coordinate Sa into system Sw attached to the work piece.

$$[M_{wd}] = \begin{bmatrix} \cos\phi_{w} & \pm\sin\phi_{w} & 0 & 0\\ \mp\sin\phi_{w} & \cos\phi_{w} & 0 & 0\\ 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 1 \end{bmatrix}$$
(20)

TABLE I - PINION AND GEAR DESIGN DATA

	PINION	GEAR
Number of teeth pinion	12	36
Dedendum angle, deg	1.5666	3.8833
Addendum angle, deg	3.8833	1.5666
Pitch angle, deg	18.4333	71.5666
Shaft angle, deg	90.0	90.0
Mean spiral angle, deg	35.0	35.0
Face width, mm (in)	25.4(1.0)	25.4 (1.0)
Mean cone		` ,
distance, mm (in)	81.05(3.191)	81.05 (3.191)
Inside radius of gear	, ,	, ,
blank, mm (in)	5.3 (0.6094)	3.0 (.3449)
Top land thickness, mm (in)	2.032 (0.080)	2.489 (.098)
Clearance, mm (in)	0.762 (0.030)	0.92964 (0.0366)

TABLE II - GENERATION MACHINE SETTINGS

	<u>PINION</u>		<u>GEAR</u>	
	Concave	Convex	Concave	Convex
Radius of cutter, r, in Blade angle, ψ , deg Vector sum, L_w Machine offset, E_m , in Cradle to cutter distance, s, in Cradle angle q, deg Ratio of roll, M_{cw} Initial cutter length, u, in Initial cutter orientation, θ , deg	2.9656 161.9543 0.038499 0.154576 2.947802 63.94 0.30838513 9.59703 126.83544	3.0713 24.33741 -0.051814 -0.1742616 2.8010495 53.926 0.32204285 7.42534 124.43689	3.0325 58.0 0.0 0.0 2.85995 59.234203 0.950864 8.12602 233.9899	2.9675 22.0 0.0 0.0 2.85995 59.234203 0.950864 7.89156 234.9545
Initial cradle orientation, ϕ_c , deg	-0.85813	-11.38663	-0.35063	-12.3384

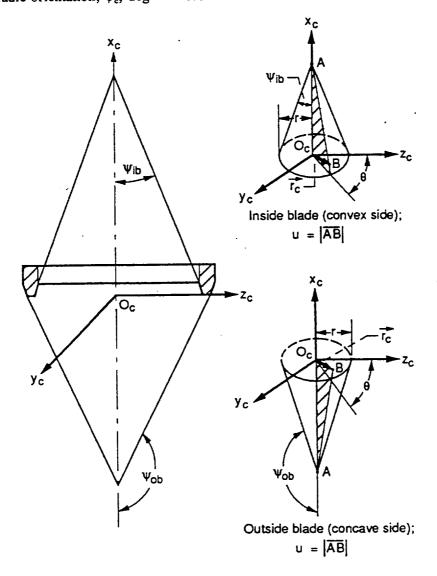


Figure 1. Cutting head cone surfaces and attached coordinate system.

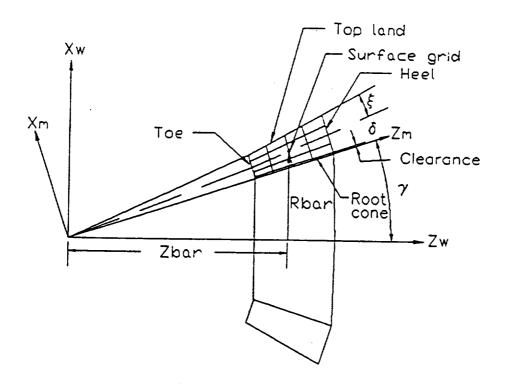


Figure 2. Projection of gear tooth with XZ plane.

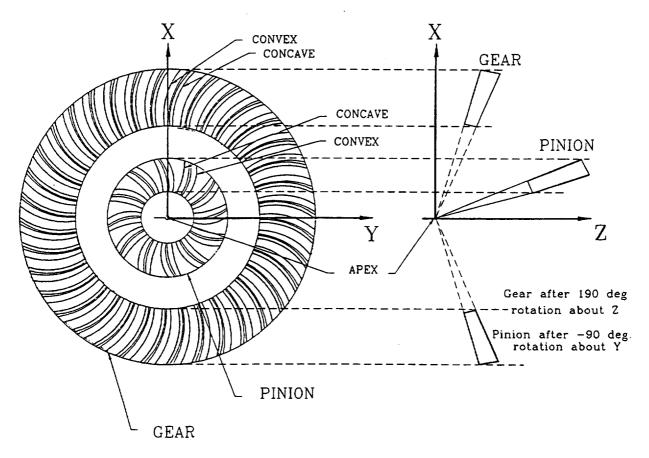


Figure 3. Orientation of gear and pinion based on solution of the system of equations, and after rotations required for mesh.

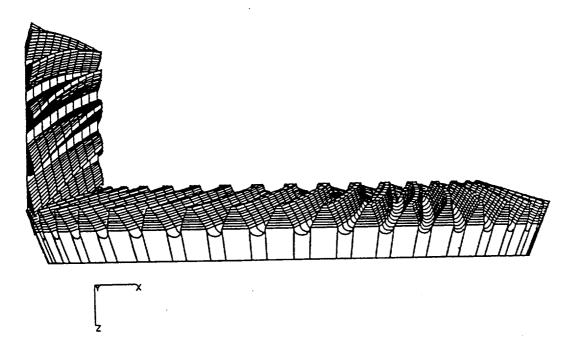


Figure 4. Complete 3D model of gear and pinion in mesh.

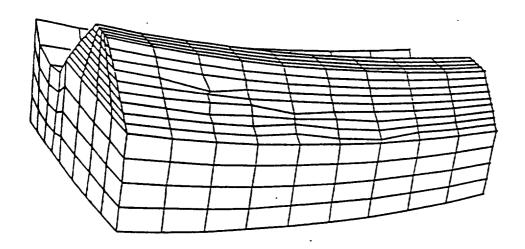


Figure 5. Distorted gear after connecting gap elements.

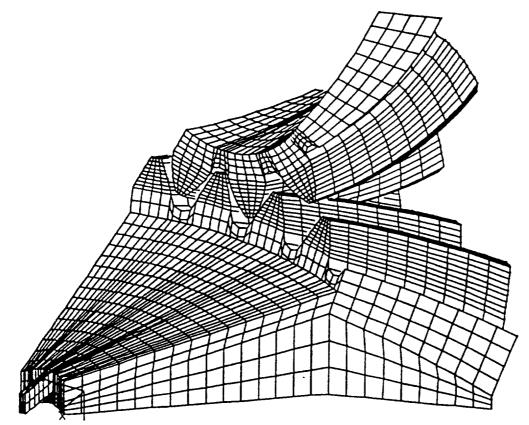


Figure 6. Seven tooth model used for finite element analysis of mesh.

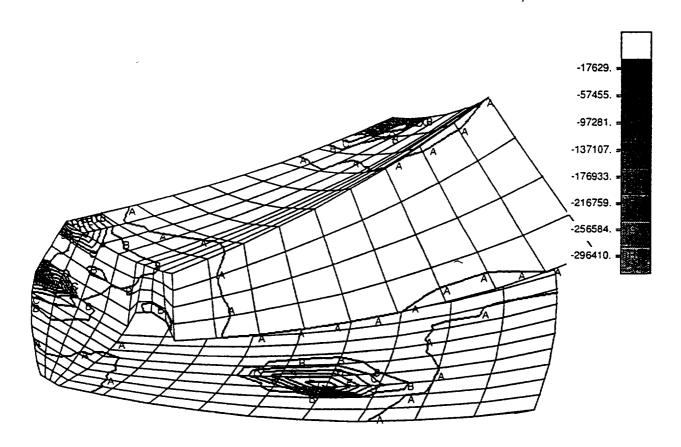


Figure 7. Stress contours in pinion tooth.

REPORT DOCUMENTATION PAGE

Form Approved
OMB No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503.

1. 4	AGENCY USE ONLY (Leave blank)	2. REPORT DATE	3. REPORT TYPE ANI	D DATES COVERED			
		May 1993	Te	chnical Memorandum			
4. 1	TTLE AND SUBTITLE	5. FUNDING NUMBERS					
	Contact Stress Analysis of S	Spiral Bevel Gears Using Nonline	ear Finite Element				
	Static Analysis	Prim Dotte Come Come Homm					
	·			WU-5056210			
6. 4	AUTHOR(S)			1L162211A47A			
	G.D. Bibel, A. Kumar, S. Re	eddy and R. Handechuh					
	U.D. Bibel, A. Kullai, S. K.						
7 6	PERFORMING ORGANIZATION NA	ME(S) AND ADDRESS(ES)		8. PERFORMING ORGANIZATION			
. .	NASA Lewis Research Center			REPORT NUMBER			
	Cleveland, Ohio 44135-3191						
	and Vehicle Propulsion Directorate	E-7876					
	U.S. Army Research Laboratory			2 .0.0			
	Cleveland, Ohio 44135-3191						
9. 9		NCY NAME(S) AND ADDRESS(ES)		10. SPONSORING/MONITORING AGENCY REPORT NUMBER			
	National Aeronautics and Space Ac Washington, D.C. 20546–0001	dministration		NAGA (19715)			
	and			NASA TM-106176			
	U.S. Army Research Laboratory			ARL-TR-158 AIAA-93-2296			
	Adelphi, Maryland 20783-1145			ALAA - 7.5 - 2.6 7.0			
11.	SUPPLEMENTARY NOTES		··· ——				
	Prepared for the 29th Joint Propuls	ion Conference and Exhibit cosponsored	by the AIAA, SAE, ASME,	and ASEE, Monterey, California, June 28–30, ddy, University of Akron, Akron, Ohio 44325;			
	and R. Handschuh, U.S. Army Veh	nicle Propulsion Directorate, NASA Lew	is Research Center. Respons	sible person, R. Handschuh, (216) 433–3969.			
122	DISTRIBUTION/AVAILABILITY S			12b. DISTRIBUTION CODE			
							
	Indentified Unlimited						
	Unclassified - Unlimited Subject Category 37						
	Subject Category 37						
12	ABSTRACT (Maximum 200 words	el					
13.	ADDINACI (MEXIMUM ZVV MORO)	" /					
	A procedure is presented for	r performing three-dimensional	stress analysis of spiral	bevel gears in mesh using the finite			
1	element method. The proces	dure involves generating a finite	element model by solv	ing equations that identify tooth surface			
	coordinates. Coordinate tran	sformations are used to orientate	e the gear and pinion fo	r gear meshing. Contact boundary			
	conditions are simulated wit	th gap elements. A solution techn	nique for correct orients	ation of the gap elements is given.			
	Example models and results	are presented.					
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14.	SUBJECT TERMS	15. NUMBER OF PAGES					
Gears; Gear teeth; Mechanical drives				16. PRICE CODE A03			
17	SECURITY CLASSIFICATION	18. SECURITY CLASSIFICATION	19. SECURITY CLASSIFICA				
۱"	OF REPORT	OF THIS PAGE	OF ABSTRACT				
I	Unclassified	Unclassified	Unclassified	1			